

I. Antoniadis

CERN

Physics with
magnetized branes

String Phenomenology 2008

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Outline

- Framework

Type I string with internal magnetic fields

- Moduli stabilization

Oblique magnetic fluxes

- Supersymmetry breaking

D-term gauge mediation

- A SUSY $SU(5)$ GUT with stabilized moduli

General framework

Type I string theory with magnetic fluxes on 2-cycles of the compactification manifold

- Dirac quantization: $H = \frac{m}{nA} \equiv \frac{p}{A}$

H : constant magnetic field

m : units of magnetic flux

n : brane wrapping

A : area of the 2-cycle

- Spin-dependent mass shifts for charged states

\Rightarrow SUSY breaking

- Exact open string description:

$qH \rightarrow \theta = \arctan qH\alpha'$ weak field \Rightarrow field theory

- T-dual representation: branes at angles

(m, n) : wrapping numbers around the 2-cycle directions

Moduli stabilization with 3-form fluxes:
significant progress but

- no exact string description
low energy SUGRA approximation
- fix only complex structure

Type I with internal magnetic fluxes:
alternative/complementary approach

- exact string description
- Kähler class stabilization
 T^6 : all geometric moduli fixed
- natural implementation in intersecting
D-brane models

Magnetic fluxes can be used to stabilize moduli

I.A.-Maillard '04, I.A.-Kumar-Maillard '05, '06

e.g. T^6 : 36 moduli (geometric deformations)

internal metric: $6 \times 7/2 = 21 = 9 + 2 \times 6$

type IIB RR 2-form: $6 \times 5/2 = 15 = 9 + 2 \times 3$

complexification \Rightarrow $\begin{cases} \text{Kähler class} & J \\ \text{complex structure} & \tau \end{cases}$

9 complex moduli for each

magnetic flux: 6×6 antisymmetric matrix F

complexification \Rightarrow

$F_{(2,0)}$ on holomorphic 2-cycles: potential for τ

$F_{(1,1)}$ on mixed (1,1)-cycles: potential for J

T^6 parametrization/complexification

$$x^i \equiv x^i + 1 \quad y_i \equiv y_i + 1 \quad i = 1, 2, 3$$

$$z^i = x^i + \tau^{ij} y_j$$

τ : 3×3 complex structure matrix

$\delta g_{i\bar{j}}$: Kähler deformations

$$\rightarrow J = \delta g_{i\bar{j}} i dz_i \wedge d\bar{z}_j$$

W : covering map

of the brane world-volume over T^6

$N = 1$ SUSY conditions:

1. $F_{(2,0)} = 0 \Rightarrow \tau$

$$\tau^\top p_{xx} \tau - (\tau^\top p_{xy} + p_{yx} \tau) + p_{yy} = 0$$

2. $J \wedge J \wedge F_{(1,1)} = F_{(1,1)} \wedge F_{(1,1)} \wedge F_{(1,1)} \Rightarrow J$

vanishing of a Fayet-Iliopoulos term

$$\xi \sim F \wedge F \wedge F - J \wedge J \wedge F$$

e.g. $T^6 = \prod_{i=1}^3 T_i^2 \leftarrow$ orthogonal 2-torus

$$\tau_i = iR_i^x / R_i^y \quad J_i = R_i^x R_i^y \quad H_i^a = F_i^a / J_i$$

$$H_1 + H_2 + H_3 = H_1 H_2 H_3 \Leftrightarrow \theta_1 + \theta_2 + \theta_3 = 0$$

3. $\det W(J \wedge J \wedge J - J \wedge F \wedge F) > 0$

action positivity

Main ingredients for moduli stabilization

- “oblique” (non-commuting) magnetic fields
⇒ fix off-diagonal components of the metric
e.g. can be made diagonal
- Non linear DBI action ⇒ fix overall volume
not valid in six dimensions: $J \wedge F = 0$

Stabilization of RR moduli

- Kähler class: absorbed by massive $U(1)$'s
kinetic mixing with magnetized $U(1)$'s
10d : $dC_2 \wedge \star(A^a \wedge \langle F^a \rangle)$
⇒ need at least 9 brane stacks
- Complex structure: get potential
through mixing with NS moduli

Bianchi-Trevigne '05

Stack #	Fluxes	Fixed moduli	5 – brane localization
#1 $N_1 = 1$	$(F_{x_1 y_2}^1, F_{x_2 y_1}^1) = (1, 1)$	$\tau_{31} = \tau_{32} = 0$ $\tau_{11} = \tau_{22}$ $\text{Re}J_{1\bar{2}} = 0$	$[x_3, y_3]$
#2 $N_2 = 1$	$(F_{x_1 y_3}^2, F_{x_3 y_1}^2) = (1, 1)$	$\tau_{21} = \tau_{23} = 0$ $\tau_{11} = \tau_{33}$ $\text{Re}J_{1\bar{3}} = 0$	$[x_2, y_2]$
#3 $N_3 = 1$	$(F_{x_1 x_2}^3, F_{y_1 y_2}^3) = (1, 1)$	$\tau_{13} = 0, \tau_{11}\tau_{22} = -1$ $\text{Im}J_{1\bar{2}} = 0$	$[x_3, y_3]$
#4 $N_4 = 1$	$(F_{x_2 x_3}^4, F_{y_2 y_3}^4) = (1, 1)$	$\tau_{12} = 0$ $\text{Im}J_{2\bar{3}} = 0$	$[x_1, y_1]$
#5 $N_5 = 1$	$(F_{x_1 x_3}^5, F_{y_1 y_3}^5) = (1, 1)$	$\text{Im}J_{1\bar{3}} = 0$	$[x_2, y_2]$
#6 $N_6 = 1$	$(F_{x_2 y_3}^6, F_{x_3 y_2}^6) = (1, 1)$	$\text{Re}J_{2\bar{3}} = 0$	$[x_1, y_1]$

Last column: 5-brane charge localization on the 2-cycles $[x_i, y_i]$

Fix areas of the 3 T^2 's \Rightarrow add 3 more stacks:

Stack #	Multiplicity	Fluxes
#7	$N_7 = 1$	$(F_{x_1y_1}^7, F_{x_2y_2}^7, F_{x_3y_3}^7) = (-4, -4, 3)$
#8	$N_8 = 2$	$(F_{x_1y_1}^8, F_{x_2y_2}^8, F_{x_3y_3}^8) = (-3, 1, 1)$
#9	$N_9 = 3$	$(F_{x_1y_1}^9, F_{x_2y_2}^9, F_{x_3y_3}^9) = (-2, 3, 0)$

$$\Rightarrow \begin{pmatrix} F_1^7 & F_2^7 & F_3^7 \\ F_1^8 & F_2^8 & F_3^8 \\ F_1^9 & F_2^9 & F_3^9 \end{pmatrix} \begin{pmatrix} J_2 J_3 \\ J_1 J_3 \\ J_1 J_2 \end{pmatrix} = \begin{pmatrix} F_1^7 F_2^7 F_3^7 \\ F_1^8 F_2^8 F_3^8 \\ F_1^9 F_2^9 F_3^9 \end{pmatrix}$$

here: $i = 1, 2, 3 \equiv i\bar{i}$

$$\Rightarrow \tau_{ij} = i\delta_{ij} \quad (J_{x_1y_1}, J_{x_2y_2}, J_{x_3y_3}) = 4\pi^2\alpha' \sqrt{\frac{3}{22}}(44, 66, 19)$$

• large volume:

- rescale all fluxes and all $J_i \Rightarrow$ three large T^2
tadpole conditions remain invariant

Tadpole conditions

$$Q_9 = \sum_a N_a \det W_a = 16 \leftarrow \text{O9 charge}$$

$$Q_5 = \sum_a N_a \det W_a \epsilon^{\alpha\beta\gamma\delta\sigma\tau} p_{\gamma\delta}^a p_{\sigma\tau}^a = 0$$

$$\forall \text{ 2-cycle } \alpha, \beta = 1, \dots, 6$$

SUSY + tadpole conditions seem incompatible

- use 9 magnetized branes to fix all moduli

impose SUSY conditions

- introduce an extra brane(s)

to satisfy RR tadpole cancellation

\Rightarrow dilaton potential from the FI D-term

\Rightarrow two possibilities:

- keep SUSY by turning on charged scalar VEVs

I.A.-Kumar-Maillard '06

D-term condition (2) is modified to:

$$qv^2(J \wedge J \wedge J - J \wedge F \wedge F) = -(F \wedge F \wedge F - F \wedge J \wedge J)$$

- EFT validity $\Rightarrow v < 1$ in string units
- Infinite family of (large volume) solutions

invariance: $\{F_a, J\} \rightarrow \{\Lambda F_a, \Lambda J\}$ for $\Lambda \in \mathbb{N}$

- fixing the dilaton?

combine magnetic and 3-form fluxes

3-brane charge $\Rightarrow T^6/\mathbb{Z}_2$ with O3 planes

magnetized D7-branes

Tadpole cancellations + fix charged scalar VEVs

Stack #	Multiplicity	Fluxes
#7	$N_7 = 1$	$(F_{x_1y_1}^7, F_{x_2y_2}^7, F_{x_3y_3}^7) = (-4, -4, 3)$
#8	$N_8 = 2$	$(F_{x_1y_1}^8, F_{x_2y_2}^8, F_{x_3y_3}^8) = (-3, 1, 1)$
#9	$N_9 = 3$	$(F_{x_1y_1}^9, F_{x_2y_2}^9, F_{x_3y_3}^9) = (-2, 3, 0)$
#10	$N_{10} = 2$	$(F_{x_1y_1}^{10}, F_{x_2y_2}^{10}, F_{x_3y_3}^{10}) = (5, 1, 2)$
#11	$N_{11} = 2$	$(F_{x_1y_1}^{11}, F_{x_2y_2}^{11}, F_{x_3y_3}^{11}) = (0, 4, 1)$

$$\Rightarrow \tau_{ij} = i\delta_{ij} \quad (J_{x_1y_1}, J_{x_2y_2}, J_{x_3y_3}) = 4\pi^2\alpha' \sqrt{\frac{3}{22}}(44, 66, 19)$$

$$v_{10}^2\alpha' \simeq \frac{0.71}{q} \simeq 0.35 \quad v_{11}^2\alpha' \simeq \frac{0.31}{q} \simeq 0.15$$

v_{10}, v_{11} : antisymmetric reps ($q = 2$) \Rightarrow

$$SU(2) \times SU(3) \times U(2)^2 \rightarrow SU(2) \times SU(3) \times SU(2)^2$$

- break SUSY in a dS or AdS vacuum

I.A.-Derendinger-Maillard to appear

General form of the localized dilaton potential:

$$V(\phi, d) = \frac{e^{-\phi}}{g^2} \left\{ \left(\sqrt{1 - d^2} - 1 \right) + \xi d + \delta T \right\}$$

DBI action
FI-term

d : D-auxiliary in $2\pi\alpha'$ -units

δT : tension leftover RR tadpole cancellation

$$\Rightarrow \delta T = 1 - \sqrt{1 - \xi^2}$$

$$d \text{ elimination } \Rightarrow d = \frac{\xi}{\sqrt{1 + \xi^2}}$$

$$V_{\min} = \delta \bar{T} e^{-\phi} \quad ; \quad \delta \bar{T} = \sqrt{1 + \xi^2} - \sqrt{1 - \xi^2}$$

Dilaton fixing:

1) by 3-form fluxes in a SUSY way

⇒ dS vacuum with positive energy

D-term uplifting possible from flat space

2) add a 'non-critical' (bulk) dilaton potential

⇒ AdS vacuum with tunable string coupling

$$V_{\text{non-crit}} = \delta c e^{-2\phi}$$

central charge deficit

minimization of $V = V_{\text{non-crit}} + V_{\text{min}} \Rightarrow \delta c < 0$

$$e^{\phi_0} = -\frac{2\delta c}{3\delta T} \quad V_0 = \frac{\delta c^3}{3\delta T^2} \quad R_0 = -\delta T e^{3\phi_0}$$

curvature in Einstein frame

e.g. replace a free coordinate by a CFT minimal model

with central charge $1 + \delta c$

D-term SUSY breaking \Rightarrow

problem with Majorana gaugino masses

- lowest order: exact R-symmetry
- higher orders: suppressed by the string scale

I.A.-Taylor '04, I.A.-Narain-Taylor '05

However in toroidal models:

- gauge multiplets have extended SUSY
- \Rightarrow Dirac gaugino masses without \mathcal{R}
- non chiral intersections have $N = 2$ SUSY

\Rightarrow Higgs in $N = 2$ hypermultiplet

\Rightarrow New gauge mediation mechanism

I.A.-Benakli-Delgado-Quiros '07

Spectrum multiplicities

$$(N_a, \bar{N}_b): I_{ab} = \det W_a \det W_b \int_{T^6} (F_{(1,1)}^a - F_{(1,1)}^b)^3$$

$$(N_a, N_b): I_{ab^*} \leftarrow F^{b^*} = -F^b$$

$$T^6 = \prod_i T_i^2 \Rightarrow I_{ab} = \prod_i (m_i^a n_i^b - n_i^a m_i^b)$$

$$I_{aa^*} = \prod_i \left\{ \frac{1}{2} (2m_i^a n_i^a \mp 2m_i^a) \pm 2m_i^a \right\}$$

number of intersections along orientifold axis $(0, x)$

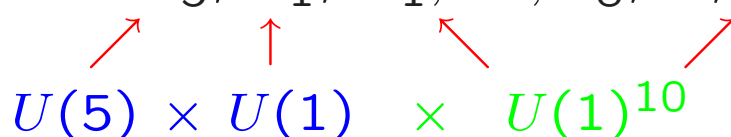
$$= \begin{cases} \text{Antisymmetric} : \frac{1}{2} \left(\prod_i 2m_i^a \right) \left(\prod_j n_j^a + 1 \right) \\ \text{Symmetric} : \frac{1}{2} \left(\prod_i 2m_i^a \right) \left(\prod_j n_j^a - 1 \right) \end{cases}$$

- non-chiral multiplicity: extract the vanishing factors
- $I_{ab^*} = 0 \rightarrow I_{ab}$ even \Rightarrow
 - odd nb of generations: constant NS B -field
 - quantization \rightarrow magnetic fluxes m half-integers

SUSY $SU(5)$ with stabilized moduli

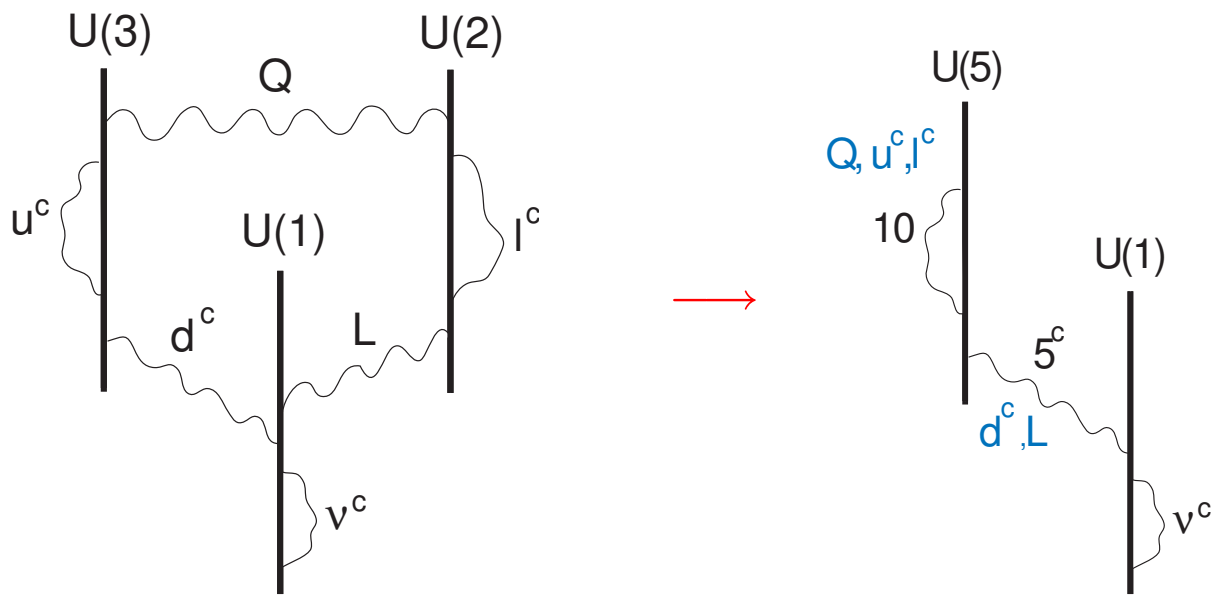
I.A.-Panda-Kumar '07

12 brane-stacks: $U_5, U_1, O_1, \dots, O_8, A, B$
 $U(5) \times U(1) \times U(1)^{10}$



winding matrix $W = \mathbf{1}$, B -field $B_{x_i y_i} = \frac{1}{2}$

- $I_{U_5 U_5^*} = I_{U_5^* U_1} = 3 \Rightarrow 3$ generations ($\mathbf{10} + \bar{\mathbf{5}}$)
- $I_{U_5 U_1} = 0 \Rightarrow$ Higgs pairs ($\mathbf{5} + \bar{\mathbf{5}}$)
- $I_{U_5 a} + I_{U_5 a^*} = 0, \forall a \neq U_5, U_1$
 \Rightarrow no other $SU(5)$ chiral states
- O_1, \dots, O_8 : set of oblique fluxes for $B \neq 0$
with diagonal induced 5-brane tadpoles



$$\begin{aligned}
 Q & \quad (3, 2; 1, 1, 0)_{1/6} \\
 u^c & \quad (\bar{3}, 1; 2, 0, 0)_{-2/3} \\
 d^c & \quad (\bar{3}, 1; -1, 0, \varepsilon_d)_{1/3} \\
 L & \quad (1, 2; 0, -1, \varepsilon_L)_{-1/2} \\
 l^c & \quad (1, 1; 0, 2, 0)_1 \\
 \nu^c & \quad (1, 1; 0, 0, 2\varepsilon_\nu)_0
 \end{aligned}$$

$$Y_A = -\frac{1}{3}Q_3 + \frac{1}{2}Q_2$$

$$\Rightarrow \sin^2 \theta_W = \frac{1}{2 + 2\alpha_2/3\alpha_3} \Big|_{\alpha_2=\alpha_3} = \frac{3}{8}$$

- SUSY conditions on $U_5, O_1, \dots, O_8 \Rightarrow$
fix all geometric moduli to diagonal metric
 $U(1)^9$ massive (absorb the RR Kähler moduli)
 - Tadpole cancellation \Rightarrow add branes A, B
 - SUSY D-flatness on $U_1, A, B \Rightarrow$
charged scalar VEVs $\neq 0$ on their intersections:
 - satisfy perturbativity constraint
 - break $U(1)^3$
- \Rightarrow leftover gauge group: $SU(5)$
- gauge non-singlet chiral spectrum:
- three generations of quarks + leptons

Conclusions

Internal magnetic fields:

simple framework, exact string description,
 $N = 1$ SUSY with chiral fermions

Moduli stabilization: 'oblique' magnetic fluxes

general: Kähler \Rightarrow complem. to 3-form fluxes

toroidal: all geometric + eventually the dilaton

Model building

natural implementation in intersecting branes

D-term SUSY breaking \Rightarrow

new mechanism of gauge mediation

Dirac gauginos, $N = 2$ Higgs potential