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# Type IIB Flux Vacua via the String Worksheet

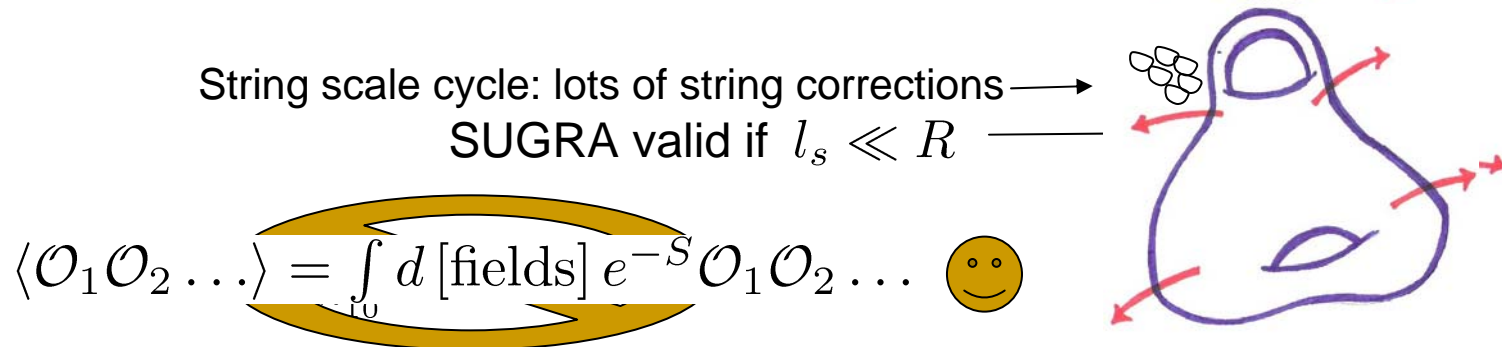
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# Motivation: Shortcomings and Expectations

- How to connect with reality? Flux compactifications are important
- Approaches typically confined to SUGRA. Need large volume limit to control  $\alpha'$

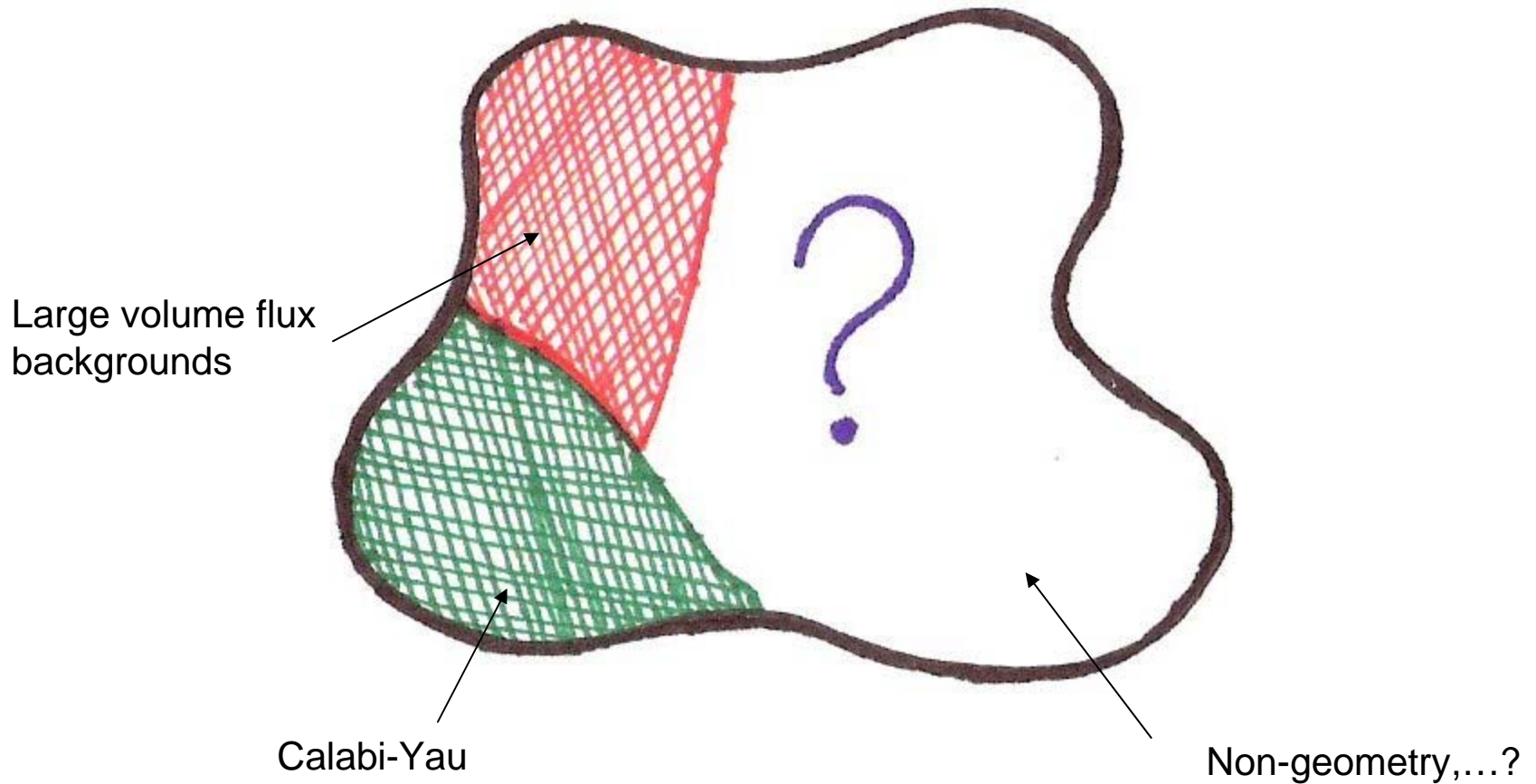


What if a cycle approaches string scale? ***Need a string description!***

- How will string theory change our SUGRA intuition?
  - Generic string solutions are expected to be string scale
  - Phenomenologically desirable to have no moduli  $\rightarrow$  hard in SUGRA
  - Are there new solutions not seen in SUGRA (eg. Non-geometric..?) Such new solutions may be phenomenologically interesting

# Type II String Theory Vacua

Likely still have much to uncover beyond SUGRA



# How to Go Beyond Supergravity?

- Traditionally, string descriptions of RR fluxes are hard & not well studied
- Three main approaches
  - Ramond-Neveu-Schwarz (RNS)
    - RR vertex operators have branch cuts, half integral picture, ...
  - Green-Schwarz (GS)
    - No covariant quantization
    - Light cone gauge is inconsistent for general flux vacua
  - D=4 Hybrid (*Berkovits,...*)

$$\text{GS}_{d=4} \oplus \text{RNS}_{\mathcal{M}_6}$$

- SO(3,1) covariant quantization
- Circumvents the above problems nicely
- Subjected to many tests (spectrum, scattering amplitudes ... )
- Well suited to flux compactifications

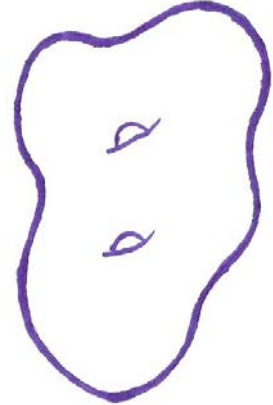
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# Outline

- ☑ 1. Motivation: Why Do We Care About String Compactifications?
- 2. ***Some Lessons from Supergravity***
- 3. Flux Vacua in the Hybrid
- 4. Physical Effects and Applications
- 5. Conclusions and Outlook

# Some Lessons from Supergravity: $CY_3$

- Without fluxes:  $M_6 = CY_3$ 
  - Preserves  $N = 2$  spacetime supersymmetry.
  - Field content is given by KK reduction on the  $CY_3$ 
    - Supergravity Multiplet
    - $h^{2,1}$  Vector Multiplets (complex structure moduli)
    - $h^{1,1} + 1$ ermultiplets (Kahler moduli and dilaton)



# Some Lessons from Supergravity: Conformally $CY_3$

- Simple Class of Solutions with  $G_3 = F_3 - \tau H_3$

- Supersymmetry broken to  $N = 1$
- SUSY  $\Rightarrow G_3$  is (2,1)
- Moduli lifted by:

$$W = \int G_3 \wedge \Omega$$

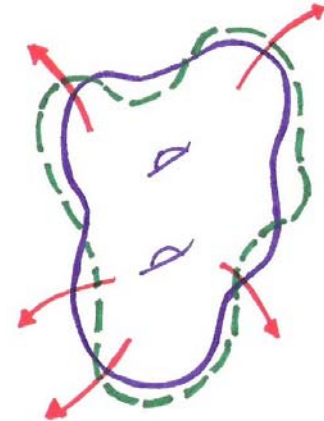
- Geometry backreacts:

$$ds^2 = e^{2A(y)} \eta_{\mu\nu} dx^\mu dx^\nu + g_{ij} dy^i dy^j \quad \text{with} \quad \square_{CY} A(y) = g_s^2 |G_{2,1}|^2 + \dots$$

- Spacetime filling five-form related to warp factor  $F_{\mu\nu\rho\tau i} = \epsilon_{\mu\nu\rho\tau} \partial_i A$

- We study these backgrounds in string theory

- Study non-compactly supported fluxes (evade tadpole, quantization)
- Hence, work perturbatively in fluxes
- SUGRA is also valid  $\rightarrow$  give us a concrete check of our approach



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# String Theory for Flux Vacua: D=4 Hybrid

- Hybrid originally formulated on  $\mathbb{R}^{3,1} \times \text{CY}_3$  with field content  $\text{GS}_{d=4} \oplus \text{RNS}_{\mathcal{M}_6}$

- Understandable as field redefinition of an N=1 critical RNS string:

- $\text{GS}_{d=4}$  redefinition of RNS D=4 & ghost variables

$$(X^\mu, \psi_L^\mu, \psi_R^\mu, b, c, \beta, \gamma) \rightarrow (X^\mu, \theta_L, \bar{\theta}_L, p_L, \bar{p}_L, \rho_L) + \text{RM}'\text{s}$$

- $\text{RNS}_{\mathcal{M}_6}$  usual RNS CY variables. Decoupled from D=4 sector.

- Worldsheet Action

$$S = \int d^2z [\partial X^\mu \bar{\partial} X_\mu + p_{L,\alpha} \bar{\partial} \theta_L^\alpha + \bar{p}_{L,\dot{\alpha}} \partial \bar{\theta}_L^{\dot{\alpha}} + \text{RM}'\text{s}] + S_{\text{chiral}} + S_{\text{CY}}$$

- Comments:

- Spacetime fermions have no branch cuts => manifest spacetime SUSY
- Even though internal theory is RNS, we show how it can describe RR fluxes
- $\text{RNS}_{\mathcal{M}_6}$  described by (2,2) c = 9 SCFT
- BRST + conformal invariance of N=1 RNS string  $\Leftrightarrow$   $\text{GS}_{d=4}$  is a (2,2) SCFT.  
=> Entire worldsheet theory  $\text{GS}_{d=4} \oplus \text{RNS}_{\mathcal{M}_6}$  is a (2,2) SCFT.
- (2,2) worldsheet superconformal invariance required for theory to be physically well-defined. We use it as our guiding principle

# String Theory for Flux Vacua: Flux Vertex Operators

- Three-form fluxes. By KK reducing on the CY:

- $F_3 = \sum_{p=1}^{h^{2,1}} F_p^{(2,1)} \omega_{2,1}^p + \text{c.c.}$

- $H_3 = \sum_{p=1}^{h^{2,1}} H_p^{(2,1)} \omega_{2,1}^p + \text{c.c.}$

- Map RNS vertex operators to Hybrid. Trick: internal fluxes correspond to spacetime auxiliary fields

- For example:  $F_3$

$$\mathcal{V}_{RNS}^p = e^{-\frac{1}{2}\phi_L - \frac{1}{2}\phi_R} \epsilon^{\alpha\beta} \sum_{L,\alpha} \sum_{R,\beta} \Psi_{RR}^p \longrightarrow \mathcal{V}_{\text{Hybrid}} = \theta_L \theta_R F_p^{(2,1)} \Omega_{1,1}^p$$

- $p = 1, \dots, h^{2,1}$  labels the  $(2,1)$  cohomology elements
- $\Psi_{RR}^p$  is RR ground state corresponding to  $p$ th cohomology element
- $\Omega_{1,1}^p$  is the (c,c) element attained by spectral flow of  $\Psi_{RR}^p$
- $\mathcal{V}_{\text{Hybrid}}$  has no branch cuts. May be integrated into the Hybrid action!

# String Theory for Flux Vacua: Flux Vertex Operators

- Have also written down vertex operators for other possible internal fluxes:

- $H_3$ :

$$\mathcal{V}_{H_3} = i(\delta\Gamma^p - \frac{1}{2}H^p) \theta_L^2 \Omega_{(1,1)}^p + i(\delta\Gamma^p + \frac{1}{2}H^p) \theta_R^2 \Omega_{(1,1)}^p + e^{-\rho_L} E_L + e^{-\rho_R} E_R,$$

where  $\Gamma^p$  is the correction to the Levi-Civita connection,  $e^{-\rho_{L,R}} E_{L,R}$  is the complexified metric in a certain picture

- $F_1$  and spacetime filling  $F_5$ :

$$\mathcal{V} = \theta_L \theta_R \bar{\theta}_R^2 (F_{1a} + iF_{5a}) \Omega_{1,0}^a + \theta_L \theta_R \bar{\theta}_L^2 (F_{1b} + iF_{5b}) \Omega_{0,1}^b + \dots$$

- $G_{2,1}$ :

$$\mathcal{V}_{G_{2,1}} = (\theta_L + i\theta_R)^2 g_s G^p \Omega_{(1,1)}^p + e^{-\rho_L} E_L + e^{-\rho_R} E_R,$$

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# Physical Effects and Applications

- Start with non-compact Calabi-Yau background
- Turn on small amount of  $G_{(2,1)}$ . Some expectations from Supergravity:
  1. Spacetime becomes warped
  2. Superpotential generated
- We see each of these effects in string theory
  - Construct the integrated vertex operator for G3 flux
$$\delta S_{G_{2,1}} = \int d^2z \mathcal{O}_{G_{2,1}} \quad \text{where} \quad \mathcal{O}_{G_{2,1}} = G_L^- G_R^- \cdot \mathcal{V}_{G_{2,1}} + \text{c.c.} \quad \text{and}$$
$$\mathcal{V}_{G_{2,1}} = (\theta_L + i\theta_R)^2 g_s G^p \Omega_{(1,1)}^p + e^{-\rho_L} E_L + e^{-\rho_R} E_R,$$
  - Deform worldsheet action by  $\delta S_{G_{(2,1)}}$
  - As spacetime SUSY manifest, easy to see this breaks half the SUSY corresponding to  $(Q_L + iQ_R)^2$

# Physical Effects and Applications: Warping & $F_5$

- The deformed action  $S_0 + \delta S_{G_3}$  is not conformally invariant at 1-loop in  $\alpha'$
- The 1-loop beta function given by the UV structure of the two point

function:

$$\mathcal{V}(z)_{G_{2,1}} \mathcal{V}(0)_{G_{2,1}} \sim \frac{(\theta_L \theta_R)(\bar{\theta}_L \bar{\theta}_R) |G^p|^2}{|z|^2} + \dots, \quad \text{Divergence breaks conformal invariance}$$

- To maintain conformal invariance we add a counter-term. Requiring D=4 Poincare, the only vertex operator with the correct  $\mu$  structure is:

$$U = (\bar{\theta}_L \sigma^\mu \theta_L)(\bar{\theta}_R \sigma^\nu \bar{\theta}_R)(\eta_{\mu\nu} A(y)) + \dots \quad \text{giving} \quad \delta S_{\text{warp}} = \int d^2 z \mathcal{Z}_L \mathcal{Z}_R \cdot U(z, \bar{z})$$

- The deformation  $\delta S_{G_3} + \delta S_{\text{warp}}$  preserves conformal invariance provided

$$\square_{CY} A(y) = g_s^2 |G^p|^2 + \dots$$

- Implies the spacetime metric has been adjusted to give precisely warping!

$$ds^2 = (1 + A + \dots) \eta_{\mu\nu} dx^\mu dx^\nu + g_{ij} dy^i dy^j$$

- Similarly, one can show conformal invariance preserved only if we have

$$F_{\mu\nu\rho\tau i} = \epsilon_{\mu\nu\rho\tau} \partial_i A$$

# Physical Effects and Applications: Superpotential

- Presence of flux => potential generated at tree level which lifts moduli
- See this in string theory by tree-level scattering amplitude

$$\langle \mathcal{V}^q \mathcal{V}^r \rangle_{S_0 + \delta S_{G_{(2,1)}}} = \langle \mathcal{V}_{G_{(2,1)}}^q \mathcal{V}^r \rangle_{S_0} \neq 0$$

$\mathcal{V}^p$  = vertex operator for complex structure modulus

- In a  $CY_3$  background,  $SL(2, \mathbb{C})$  and worldsheet SUSY =>  $\langle \mathcal{V}^q \mathcal{V}^r \rangle_{S_0} = 0$
- Flux background inserts a vertex operator, rendering the amplitude non-zero
- Manifest spacetime SUSY => scattering amplitude automatically computes a superpotential

$$\mathcal{W} = 3 \int d^4x d^2\theta^- g_s G_{(2,1)}^p \mathcal{V}^q(x, \theta^-) \mathcal{V}^r(x, \theta^-) C_{pqr}$$

↑  
Integration over zero modes  
and unbroken SUSY
← Topological  
invariant of CY

- This may be recast in a more familiar form:

$$\mathcal{W} = \int G \wedge \delta\Omega.$$

# Conclusions and Outlook

## ■ Summary:

- Important to have string theory description of flux vacua
- This may lead to new string solutions, which are phenomenologically viable (no moduli, string scale, understanding of the landscape...)
- We have shown how to identify flux vertex operators in the Hybrid
- Computed using string theory effects well-known in supergravity

## ■ Future and Current Work:

- Tip of the iceberg: many *computable* interesting physical effects.
- Need to understand finite flux deformations and orientifolding (compact solutions)
- Construction of a Hybrid GLSM (*work in progress with J. Park, C. Quigley, D. Robbins, S. Sethi*)
- Eventually understand vacua that are string scale: eg. non-geometric, no volume modulus.