

**Math 410**  
**Assignment 6**

**Dr. DeTurck**  
**Due Tuesday, November 10, 2009**

**Reading:** Textbook, Chapter 3 (you just have to skim section 5), also take a look at the first couple of sections of chapter 4.

**Problems to hand in:**

1. Textbook page 105, problems 8, 9, 10, 12, 14, 15(d)
2. For each of the following polynomials, determine how many of its roots lie inside the circle  $|z| = 1$ :
  - (a)  $z^6 - 5z^4 + z^3 - 2z$
  - (b)  $2z^4 - 2z^3 + 2z^2 - 2z + 9$
3. Determine the number of roots of the equation  $2z^5 - 6z^2 + z + 1 = 0$  in the region  $1 \leq |z| < 2$ .
4. Show that if  $c$  is a complex number such that  $|c| > e$ , the equation  $cz^n = e^z$  has  $n$  roots inside the circle  $|z| = 1$ .