Math 116

From Apostol, read Chapter 3, section 16. Read Chapter 4, sections 3-5, 10, 13, 14, 16, 17. Also read Chapter 1, sections 9-14. Optional: Read Chapter 3, sections 12-14 and 17; and Chapter 4, sections 1, 2, 7, 8, 11, 18, 20.

1. From Apostol,  $\S4.6$ , pages 167-168, do problem 38; in  $\S4.9$ , page 173, do problems 7 and 9; and in  $\S4.12$ , page 179, do problem 14.

2. From Apostol,  $\S1.15$ , page 70, do problems 1 (a,d,e), 2, 3, 5(a).

3. For each of the following functions f, determine whether f has a maximum value and whether it has a minimum value. If such values exist, find them and find for which values of x they are achieved. Relate your answer to the extreme value theorem.

a)  $f(x) = x^3 - 2x^2 - 4x + 1$  on the interval  $0 \le x \le 4$ .

- b) Same as (a) but on the interval 0 < x < 4.
- c)  $f(x) = 1/x^2$  if  $-1 \le x \le 1$  with  $x \ne 0$ ; and f(0) = 0.
- d) f(x) = x [x] for  $0 \le x \le 3$ .

4. Which of the following functions are differentiable at x = 0? For each one that is, find f'(0), and determine whether the function f' is continuous at x = 0.

- a)  $f(x) = \sin(1/x)$  for  $x \neq 0$ , f(0) = 0. b)  $f(x) = x \sin(1/x)$  for  $x \neq 0$ , f(0) = 0. c)  $f(x) = x^2 \sin(1/x)$  for  $x \neq 0$ , f(0) = 0.
- d)  $f(x) = x^3 \sin(1/x)$  for  $x \neq 0$ , f(0) = 0.

5. Find a function f on  $\mathbb{R}$  such that f is differentiable at x = 0 and f is discontinuous at every  $x \neq 0$ .