From Apostol, read Chapter 14, sections 8-20.

1. From Apostol, 14.7, pages 524-525: do problem 14 (Hint: adapt the previous argument in the case of an ellipse); and 14.9, pages 528-529: do problems 1, 2, 7.

2. From Apostol, 14.13, pages 535-536: do problems 2, 11, 13.

3. From Apostol, 14.15, pages 538-539: do problems 1 (do just for #1,2 of 14.9), 2, 4, 7; and 14.19, pages 543-545: do problems 1, 2(a), 4, 5.

4. Let $f : \mathbb{R} \to \mathbb{R}$ be a twice differentiable function. Parametrize the plane curve y = f(x) by F(t) = (t, f(t)), and suppose that F(a) = (a, f(a)) is an inflection point of this curve for some value of a. Prove that T'(a) = 0, where T(t) is the unit tangent vector to the curve at the point F(t). Is the principal normal vector N(a) at F(a) defined?

5. a) Find the arclength of the plane curve given parametrically by $F(t) = (2t, \frac{t^3}{3} + \frac{1}{t})$, for $1 \le t \le 3$.

b) Find the arclength of the plane curve whose graph is $y = \log \cos x$ for $0 \le x \le \pi/4$. (Here log is the natural logarithm.)

6. Consider the curve in \mathbb{R}^3 given parametrically by $F(t) = ti + t^2j + t^3k$, where i, j, k are the unit basis vectors. Find the curvature at the origin, and find all points where the curvature is zero.