# Math 312 Fall, 2015 Syllabus Prof. Murray Gerstenhaber 

August 20, 2015

The numbering of sections follows that of the text, Linear Algebra, 2nd edition by Kenneth A. Hoffman and Ray Kunze.

The heart of the course is Chapter 8 on inner product spaces, which we will cover thoroughly. While the syllabus below leaves time for Chapters 9 and 10, if we don't get to them those who wish may read and do exercises on the material for extra credit. We will skip from Chapter 3 to Chapter 5 and then take up Chapter 4 after the midterm, which is scheduled for October 20.

Our treatment of determinants will be advanced but there will be notes. You will need understand dual bases, currently scheduled for Lecture 9. The syllabus is not filled in after Thanksgiving; details will be added. To the extent that time permits, we will end with some important applications.

| TUESDAYS | THURSDAYS |
| :---: | :---: |
| Aug 25 vacation | Aug 27 Lecture 1 <br> 1.1. Fields <br> 1.2. Systems of Linear Equations <br> 1.3. Matrices and Elementary Row Operations |
| SEpt 1 Lecture 2 <br> 1.4. Row-Reduced Echelon Matrices <br> 1.5. Matrix Multiplication <br> 1.6. Invertible Matrices <br> The determinant of a $2 \times 2$ matrix. (General determinants will be covered later.) | Sept 3 Lecture 3 <br> 1.6 Invertible Matrices (cont'd) <br> 2.1 Vector Spaces <br> 2.2 Subspaces <br> quotient spaces <br> Rings and modules; Rings of matrices <br> We will introduce here some topics covered more fully in Chapter 8, in particular inner product spaces (Euclidean spaces). |
| SEPT 8 Lecture 4 <br> 2.3 Bases and Dimension | September 10 Lecture 5 <br> 2.4 Coordinates <br> 2.5 Summary of Row Equivalence |
| Sept 15 no Class Hashanah 2nd day) | September 17 Lecture 6 <br> 2.6 Computations Concerning Subspaces <br> Review |


| TUESDAYS | THURSDAYS |
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| SEpt 22 Lecture 7 <br> 3.1 Linear Transformations <br> 3.2 The Algebra of Linear Transformations <br> Linear operators on a vector space; <br> The concept of a group | SEpt 24 Lecture 8 <br> 3.3 Isomorphism <br> 3.4 Representation of Transformations by Matrices |
| Sept 29 No Class (Sukkot 2ND DAY) | Oct 1 Lecture 9 <br> 3.5 Linear Functionals <br> Dual bases; Dual transformations |
| Oct 6 Lecture 10 <br> Chapter 5. Determinants <br> Some basic concepts will simplify the treatment in the text. <br> 5.x1 Tensor and exterior products of vector spaces | Oct 8 No Class - Fall Break |
| Oct 13 Lecture 11 <br> Determinants (cont'd) | Oct 15 Lecture 12 Chapter 6. Review |
| Oct 20 MIDTERM | Oct 22 Lecture 13 <br> Chapter 4. Polynomials <br> 4.1 Algebras <br> 4.2 The algebra of Polynomials <br> 4.3 Lagrange Interpolation |
| Oct 27 Lecture 14 <br> 4.4 Polynomial Ideals <br> 4.5 The Prime Factorization of a <br> Polynomial <br> Factorization over the real and over the complex numbers | Oct 29 Lecture 14 <br> Chapter 6. Elementary Canonical Forms |


| TUESDAYS | THURSDAYS |
| :---: | :---: |
| Nov 3 (Election Day) Lecture 15 Chapter 6. Elementary Canonical Forms 6.1 6.2 6.3 6.4 | Nov 5 Lecture 16 6.5 6.6 6.7 6.8 |
| Nov 10 Lecture 17 <br> Chapter 7. The Rational and Jordan Forms | Nov 12 Lecture 18 <br> Chapter 7. The rational and Jordan Forms |
| Nov 17 Lecture 19 Chapter 8. Inner Product Spaces | Nov 19 Lecture 20 Chapter 8. Inner Product Spaces |
| Nov 24 Lecture 21 Chapter 8. Inner Product Spaces | Nov 26 Thanksgiving Day |
| Dec 1 Lecture 22 | Dec 3 Lecture 23 |
| Dec 8 Lecture 24 Last Class | Dec 10 Reading Day Review |

## MONDAY, DEC 14 FINAL EXAM

