## Math 114 Calculus, Part II

Functions of several variables, vector-valued functions, partial derivatives and applications, double and triple integrals, conic sections, polar coordinates, vectors and vector calculus, first order ordinary differential equations. Applications to physical sciences. Use of symbolic manipulation and graphics software in calculus.

Text: Thomas' Calculus Early Transcendentals Custom Edition for the University of Pennsylvania Pearson 2018. Package ISBN : 3 Semester access 978-0134786254 or 1 Semester access 978-0135901410
Section Title Core Problems

|  | Three-Dimensional Coordinate <br> Systems | $5,19,25,36,47,54,65$. |
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| 12.1 | Vectors | $1,11,20,24,25,35,45,49,53$. |
| 12.2 | The Dot Product | $3,11,19,26,29,43,50$. |
| 12.4 | The Cross Product | $5,9,15,21,26,27,31,37,44,50$. |
| 12.5 | Lines and Planes in Space | $5,15,23,29,35,43,57,62,67,70,77$. |
| $11.6+12.6$ | Conic Sections, Cylinders and <br> Quadric Surfaces | Section 11.6:5,6, 7, 8, 9, 21, 34, 70. <br> Section $12.6: 1-12,17,25,27,32,46$. |


| 13.1 | Curves in Space and Their <br> Tangents | $5,11,15,22,26,38,42$. |
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| 13.2 | Integrals of Vector Functions; <br> Projectile Motion | $1,13,22,25,34,37,41$. |
| 13.3 | Arc Length in Space | $5,12,17,19$. |
| 13.4 | Curvature and Normal Vectors <br> of a Curve | $3,7,12,19,24$. |
| 13.5 | Tangential and Normal <br> Components of Acceleration | $2,5,8,9,17,21,26,28$ |
| 13.6 | Velocity and Acceleration in <br> Polar Coordinates | $3,8,12$. |


| 14.1 | Functions of Several Variables | $3,9,14,18,31,32,33,34,35,36,39,50$, <br> $55,62,65$. |
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| 14.2 | Limits and Continuity in Higher <br> Dimensions | $1,9,16,27,32,41,49,60,65$. |
| 14.3 | Partial Derivatives | $5,22,26,39,46,58,69,75,83,93,100$. |
| 14.4 | The Chain Rule | $3,7,12,14,25,33,37,47,51,56,59$. |
| 14.5 | Directional Derivatives and <br> Gradient Vectors | $3,8,13,21,26,29,34,39$. |
| 14.6 | Tangent Planes and <br> Differentials | $3,11,17,21,26,31,35,44,49,51,56,60$ |
| 14.7 | Extreme Values and Saddle <br> Points | $2,17,31,41,44,49,59,67$. |
| 14.8 | Lagrange Multipliers | $5,11,20,29,31,42,43$. |


| Section | Title | Core Problems |
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| 15.1 | Double and Iterated Integrals <br> over Rectangles | $1,14,21,24,29$. |
| 15.2 | Double Integrals over General <br> Regions | $1,9,19,26,35,51,57,67,71,73,78,84$. |
| 15.3 | Area by Double Integration | $3,16,19,25$. |
| $11.3+15.4$ | Polar Coordinates and Double <br> Integrals in Polar Form | Section 11.3: 17, 23, 25. <br> Section 15.4: 4, 15, 23, 33, 39, 45, 46. |
| 15.5 | Triple Integrals in Rectangular <br> Coordinates | $3,9,21,23,39,43,47$. |
| 15.6 | Moments and Centers of Mass | $1,4,8,13,22,29$. |
| 15.7 | Triple Integrals in Cylindrical <br> and Spherical Coordinates | $23,31,36,43,50,56,67,81,90,100$. |
| 15.8 | Substitutions in Multiple <br> Integrals | $1,5,11,23,26$. |


| 16.1 | Line Integrals | $9,11,14,19,22,25$. |
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| 16.2 | Vector Fields and Line Integrals | $2,7,10,19,20,27$. |
| 16.3 | Path Independence, <br> Conservative Fields, and <br> Potential Functions | $1,4,19,20,27,28,30$ a and c. |
| 16.4 | Green's Theorem in the Plane | $10,13,15,17,25,33,34$. |
| 16.5 | Surfaces and Area | $4,7,8,19,23,37,41,47$. |
| 16.6 | Surface Integrals | $2,3,7,14,17,38,39$. |
| 16.7 | Stokes' Theorem | $9,12,13,19,25$. |
| 16.8 | Divergence Theorem | $9,12,13,15,19,32$. |

SAMPLE EXAM QUESTIONS also form a part of the core, they are available from the Math Dept's Math 114 Web Page:
https://www.math.upenn.edu/undergraduate/calculus-homepages/calculus/mathematics-114

The core problems indicate the kind of basic problems you will need to be able to solve by hand. They also provide a guide to the basic level of difficulty to be expected on the final exam.

Note: All sections of Math 114 have a COMMON FINAL EXAM

