

Instructions: This quiz has 26 questions. The use of calculators is forbidden. Click on the box with the right answer. To initialise the quiz you must click on "BEGIN QUIZ." When you finish the quiz you click on "END QUIZ" in order to see your score.

Begin Quiz Answer each of the following.

- Find $\lim_{x \rightarrow a} x^2 - ax + b$, where a, b are real constants.

a	ab	b	$a^2 + b$
-----	------	-----	-----------
- Find $\lim_{x \rightarrow a} \frac{x^2 - a^2}{x - a}$, where a is a real constant.

a	$2a$	0	a^2
-----	------	-----	-------
- Let $f(x) = \begin{cases} 1 & \text{if } x \neq 1 \\ -1 & \text{if } x = 1 \end{cases}$. Which of the following assertions is true?

$\lim_{x \rightarrow 1} f(x) = 1$ and f is continuous at 1
$\lim_{x \rightarrow 1} f(x) = -1$ and f is continuous at 1
$\lim_{x \rightarrow 1} f(x) = 1$ and f is discontinuous at 1
$\lim_{x \rightarrow 1} f(x) = -1$ and f is discontinuous at 1
- If $f(x) = ax^2 - a^2x$, where a is a real constant, then $f'(a) =$

0	$2a$	a	a^2
-----	------	-----	-------
- If $y = \frac{b}{x - a}$, where a, b are real constants, then $\frac{dy}{dx} =$

$-\frac{b}{(x - a)^2}$	$\frac{b}{(x - a)^2}$	$\frac{b}{x(x - a)}$	$b(x - a)$
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6. f is a function such that $f(0) = 0$, $xf'(x) > 0$ for $x \neq 0$, and $xf''(x) > 0$ for $x \neq 0$. Which of the following could be the graph of f ?

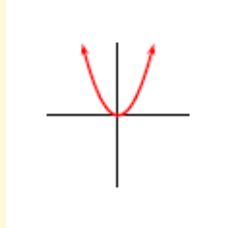


Figure 1: I

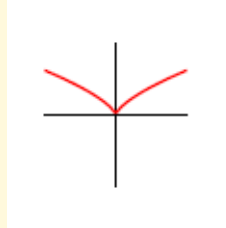


Figure 2: II

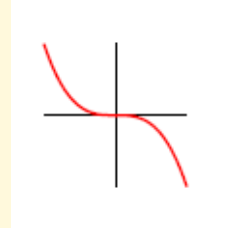


Figure 3: III

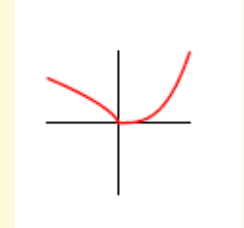


Figure 4: IV

I

II

III

IV

7. At $x = -2$, the tangent line to the graph of $y = x^3 - 2x^2 + 1$ has slope

-20

-15

20

4

8. $\int 3x^5 dx =$

$\frac{x^6}{2} + C$

$\frac{x^6}{3} + C$

$\frac{x^5}{2} + C$

$15x^2 + C$

9. By the Mean Value Theorem, between $(1, 0)$ and $(2, 1)$, the function $f(x) = x^3 - 2x^2 + 1$ has at least one point at which its derivative has the value

-1

0

1

2

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10. If $a \neq 0$ is a real constant, then $\int \csc^2 ax dx =$

$$\frac{\cot ax}{a} + C \qquad -\frac{\cot ax}{a} + C \qquad \frac{(\csc ax)^3}{a} + C \qquad \csc^3 ax + C$$

11. If $a \neq 0$ is a real constant, and $f(x) = (\sin ax)(\cos ax)$, then $f'(0) =$

$$0 \qquad a \qquad 2a \qquad a^2$$

12. If a, b, c are non-zero real constants, then $\lim_{x \rightarrow +\infty} \frac{ax^2 + bx + c}{a^2x^2 + b^2x + c} =$

$$ab \qquad a \qquad 2a \qquad \frac{1}{a}$$

13. The slope of the line tangent to the curve $x + 4y - 2y^3 - 3 = 0$ at the point $(1, 1)$ is

$$-\frac{1}{3} \qquad \frac{1}{3} \qquad \frac{1}{2} \qquad -\frac{1}{2}$$

14. The absolute maximum value of the function $f(x) = x^3 - 2x + 4$ on the interval $[-2; 2]$ is

$$4 - \frac{4}{9}\sqrt{6} \qquad \frac{4}{9}\sqrt{6} + 4 \qquad 8 \qquad 10$$

15. If $f(0) = a$ and $f(1) = b$, where a, b are real constants, then $\int_0^1 f'(x) dx =$

$$a - b \qquad b - a \qquad a + b \qquad \text{impossible to determine}$$

16. Compute the area between the curves $y = 2 - 2x - x^2$ and $y = 1 - 2x$.

$$1 \qquad \frac{2}{3} \qquad \frac{4}{3} \qquad \frac{1}{3}$$

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17. Figure 5 consists of four semicircles, two of radius 1 and two of radius $\frac{1}{2}$. If $g(x) = \int_0^x f(t)dt$, where is $g(x) \geq 0$?

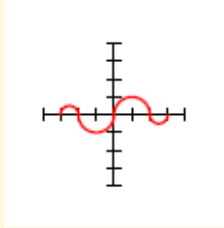


Figure 5: Problem 17.

$$[-3; 3]$$

$$[-3; -2] \cup [0; 2] \text{ only}$$

$$[0; 3] \text{ only}$$

$$[-3; -2] \cup [0; 3] \text{ only}$$

18. The number of unfilled pharmacist positions in year x is approximately

$$P(x) = -583x^3 + 2068x^2 + 323x + 2670, \quad 0 \leq x \leq 3.$$

If $x = 0$ corresponds to year 1998, in what year was the shortage of pharmacists most severe?

1998

1999

2000

2001

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19. When a stone is dropped into a pool, a circular wave moves out from the point of impact at the rate of $3a$ inches per second ($a > 0$ a real constant). How fast is the area enclosed by the wave increasing when the radius of the wave is a inches?

$2\pi a^2$ square inches per second

$3\pi a^2$ square inches per second

$4\pi a^2$ square inches per second

$6\pi a^2$ square inches per second

20. $\int_1^9 \frac{dx}{(2 + \sqrt{x})^2 \sqrt{x}} =$

$\frac{196}{10125}$

$\frac{4}{15}$

$2 \ln \frac{5}{3}$

$\frac{16}{225}$

21. If Newton's method is used to solve $x^3 - 3x^2 + 4x - 1 = 0$ with an initial guess of $x = 0$, then the second approximation is closest to

0.318

0.314

0.25

0.184

22. For which value of the real parameter a does the polynomial $x^3 + 2x + a$ have a root in the interval $[-1; 0]$?

$a = -1$

$a = 0$

$a = 10$

$a = 20$

23. If a is a real constant, then $\lim_{x \rightarrow 0} \frac{\sin ax - \tan a^2 x}{x} =$

$2a$

$-a$

$a - a^2$

a

24. $\lim_{h \rightarrow 0} \frac{\sqrt[4]{16+h} - 2}{h} =$

$\frac{1}{16}$

$\frac{1}{32}$

$\frac{1}{64}$

$\frac{1}{4}$

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25. Consider the three functions

$$a(x) = \sqrt{\frac{2-x}{x+1}}; \quad b(x) = \sqrt{2-x} + \sqrt{x+1}; \quad c(x) = \sqrt{\frac{x+1}{2-x}}$$

and the three sets of real numbers

$$I : [-1; 2] \quad II :] - 1; 2] \quad III : [-1; 2[.$$

Match each function with its domain of definition.

$$(I, a), (II, b), (III, c)$$

$$(I, b), (II, c), (III, a)$$

$$(I, b), (II, a), (III, c)$$

$$(I, c), (II, b), (III, a)$$

26. Find the volume of the solid when the region bounded by the x -axis, the y -axis, and the curve $y = x(1 - x)$ is rotated about the x -axis.

$$\frac{\pi}{30}$$

$$\frac{\pi}{15}$$

$$\frac{\pi}{6}$$

$$\frac{\pi}{60}$$

End Quiz

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