

**Question 1C.** Find the degree 4 Taylor approximation about  $x = 0$  of the function below. For your numerical answer, enter the coefficient of  $x^4$ .

$$\frac{d}{dx} \int_0^{2x} \cosh(t^2) dt$$

**Question 2A.** The value of  $\int_2^3 \frac{3x^2 - 1}{x^3 - x} dx$  can be expressed as  $\ln k$ . Determine  $k$  **without** using the substitution  $u = x^3 - x$ .

**Question 3A.** Compute the interval of convergence for the power series below.

$$\sum_{n=5}^{\infty} \frac{(x-1)^n}{2^n n (\ln n)^3}$$

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$(-1, 3]$

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$(-3, 1)$

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$[-1, 3)$

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$[-1, 3]$

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$(-1, 3)$

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$[-3, 1]$

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$(-3, 1]$

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$[-3, 1)$

**Question 4B.** For the curve given parametrically by  $x(t) = t^3 \cos \frac{1}{t}$ ,  $y(t) = t^3 \sin \frac{1}{t}$ , the arc length for  $0 \leq t \leq A$  is which of the following?

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$\frac{1}{27}(9A^2 + 1)^{3/2}$

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$\frac{1}{27}\sqrt{9A^2 + 1}$

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$[(9A^2 + 1)^{3/2} - 1]$

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$\frac{1}{27}[(9A^2 + 1)^{3/2} - 1]$

**Question 5B.** The series below converges for all values of  $p$  strictly bigger than some number  $k$ . Find  $k$ . In your written work, justify divergence when  $p = k$  and convergence when  $p > k$ .

$$\sum_{n=1}^{\infty} \left( e^{2/n^p} - 1 \right)$$

**Question 6C.** A continuous function  $f(x)$  satisfies  $0 \leq f(x)$ , for  $0 \leq x \leq 1$ . When the region between  $y = f(x)$  and the  $x$ -axis, as  $x$  goes from 0 to 1, is rotated around the  $y$ -axis, the resulting solid has volume  $8\pi$ . If  $F(x) = \int_0^x f(x)dx$  and  $\int_0^1 F(x)dx = 1$ , find  $F(1)$  (the answer is a whole number).