

# MATH 314 ASSIGNMENT 7, FALL 2016

Due in class on Friday, March 4

Part 1. Read §4.5 and §5.1–5.3 of Hoffman–Kunze

Part 2. Do and hand in the following problems in Hoffman–Kunze.

- 4.4, problem 4
- 4.5, problems 1, 2
- 5.2, problems 8, 10, 11
- 5.3, problems 4, 8

Part 3. (extra credit) Let  $E$  be a subfield of a field  $F$ , i.e.  $E$  is a subset of  $F$  which contains 0 and 1, stable under both addition and multiplication, and the inverse of every non-zero element of  $E$  is in  $E$ . Let  $f, g$  be non-zero elements of the polynomial ring  $E[x]$  in one variable  $x$ . Prove that every gcd of  $f$  and  $g$  in  $E[x]$  is also a gcd of  $f$  and  $g$  in  $F[x]$ .