AMCS 602

Problem set 7 due November 1, 2016 Dr. Epstein

Reading: We are covering the material in Chapters 22, 33, and 35 on this problem set. Page numbers below refer to *Numerical Linear Algebra* by Trefethen and Bau.

Standard problems: The following problems should be done, but do not have to be handed in.

- 1. Page 171, problem 22.2.
- 2. Page 255, problem 33.1.
- 3. Page 275, problem 35.5.

Homework assignment: The solutions to the following problems should be carefully written up and handed in.

- 1. Page 171, problem 22.1.
- 2. Page 171, problem 22.4.
- 3. Page 177, problem 23.1.
- 4. Page 255, problem 33.2.
- 5. Page 255, problem 33.3.
- 6. Page 274, problem 35.1.
- 7. Page 274, problem 35.2. Show that if S is a closed curve (or contains a closed curve) that bounds a region containing zero, then for any n, and $p_n \in P_n$, it is impossible for $||p_n||_S < 1$. How will GMRES behave for a matrix A whose spectrum "includes" S? Of course the spectrum of a finite rank matrix cannot contain a continuum; here one should imagine that m is very large and the matrix A is a finite rank approximation to an operator in an infinite dimensional space, whose spectrum includes S.
- 8. Page 274, problem 35.3.
- 9. Page 275, problem 35.4.