

Name: _____

Section: _____

Find the curvature and torsion of the curve (t, t^2, t^3) at the time $t = 0$.

$$\begin{aligned}v(t) &= (1, 2t, 3t^2) \\a(t) &= (0, 2, 6t) \\a'(t) &= (0, 0, 6)\end{aligned}$$

$$\begin{aligned}v(0) &= (1, 0, 0) \\a(0) &= (0, 2, 0) \\a'(0) &= (0, 0, 6)\end{aligned}$$

$$v(0) \times a(0) = \begin{vmatrix} i & j & k \\ 1 & 0 & 0 \\ 0 & 2 & 0 \end{vmatrix}$$

$$\begin{aligned}v(0) \times a(0) &= (0, 0, 2) \\|v(0) \times a(0)| &= 2 \\|v(0)| &= 1\end{aligned}$$

$$\kappa(0) = \frac{2}{1^3} = 2$$

$$\tau(0) = \frac{\begin{vmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 6 \end{vmatrix}}{(2)^2}$$

$$\tau(0) = \frac{12}{4} = 3$$